

HEREDITARY (BI)COREFLECTIVE SUBCATEGORIES IN CERTAIN CATEGORIES OF SEMITOPOLOGICAL GROUPS

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Let \mathbf{A} be an epireflective subcategory of the category \mathbf{STopGr} of all semitopological groups and continuous homomorphisms (all subcategories of \mathbf{STopGr} are assumed to be full and isomorphism-closed). It is well-known that a subcategory of \mathbf{A} is monoreflective in \mathbf{A} if and only if it is closed under the formation of coproducts and extremal quotient objects in \mathbf{A} . Every hereditary (closed under the formation of subgroups) coreflective subcategory of \mathbf{A} is monoreflective. Moreover, in the categories \mathbf{STopGr} and \mathbf{QTopGr} (the category of all quasitopological groups) every hereditary coreflective subcategory \mathbf{B} that contains a group with the non-indiscrete topology is also bireflective (i.e. every \mathbf{B} -coreflection is simultaneously a monomorphism and an epimorphism). In the talk we will present other examples of epireflective subcategories of \mathbf{STopGr} with this property.

Next we will focus on such epireflective subcategories \mathbf{A} of \mathbf{STopGr} that the \mathbf{A} -reflection of the discrete group of integers is one of the following:

1. a discrete group,
2. a group with a topology that is not T_0 ,
3. the group of integers with the topology generated by all of its non-trivial subgroups.

We will present new results on hereditary bireflective subcategories of \mathbf{A} and we will describe maximal hereditary coreflective subcategories of \mathbf{A} that are not bireflective in \mathbf{A} .